

MACER: Attack-Free and Scalable Robust Training via Maximizing Certified Radius

Runtian Zhai, Chen Dan, Di He, Huan Zhang

Boqing Gong, Pradeep Ravikumar, Cho-Jui Hsieh & Liwei Wang



A provable, fast and scalable adversarial defense



Provable: Model robustness can be certified

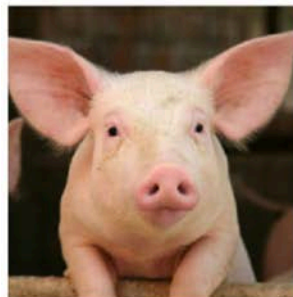


Fast: No expensive attack operation in training



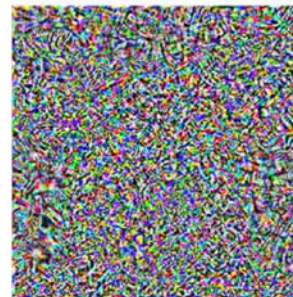
Scalable: Applicable to deep neural networks

“pig” (91%)



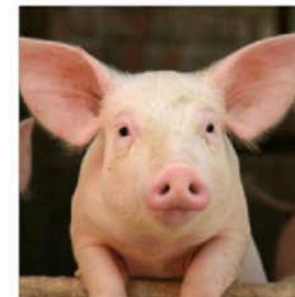
+ 0.005 x

noise (NOT random)



=

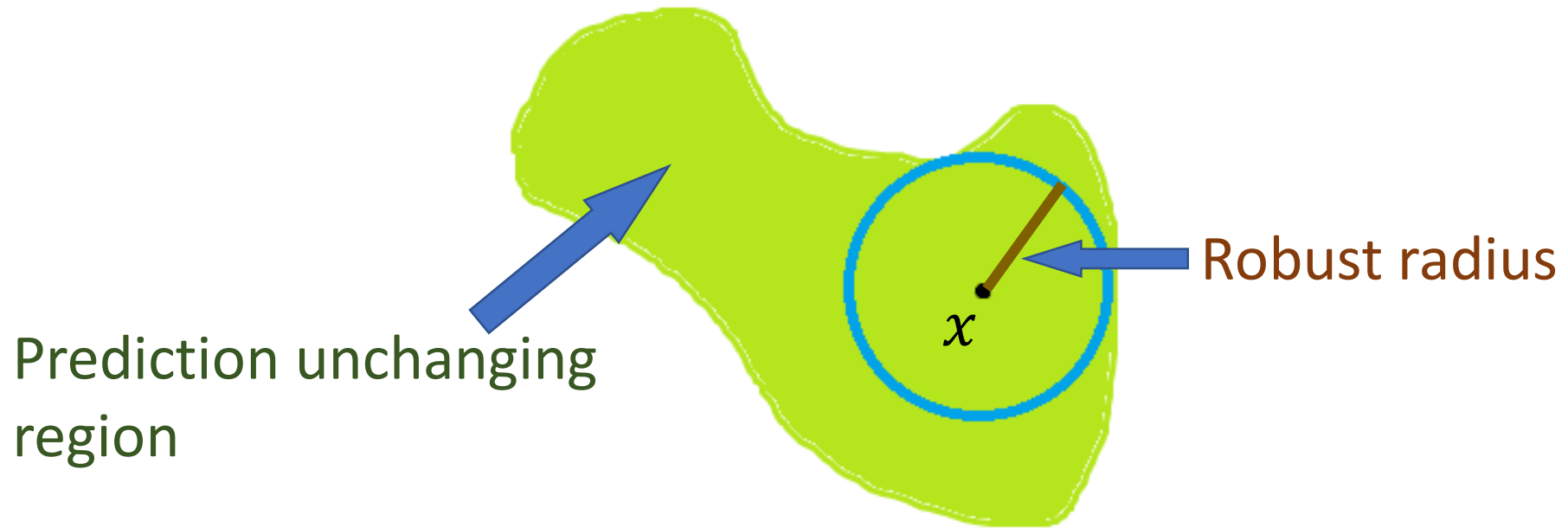
“airliner” (99%)



Robust radius

Training a robust model \Leftrightarrow Maximizing the robust radius

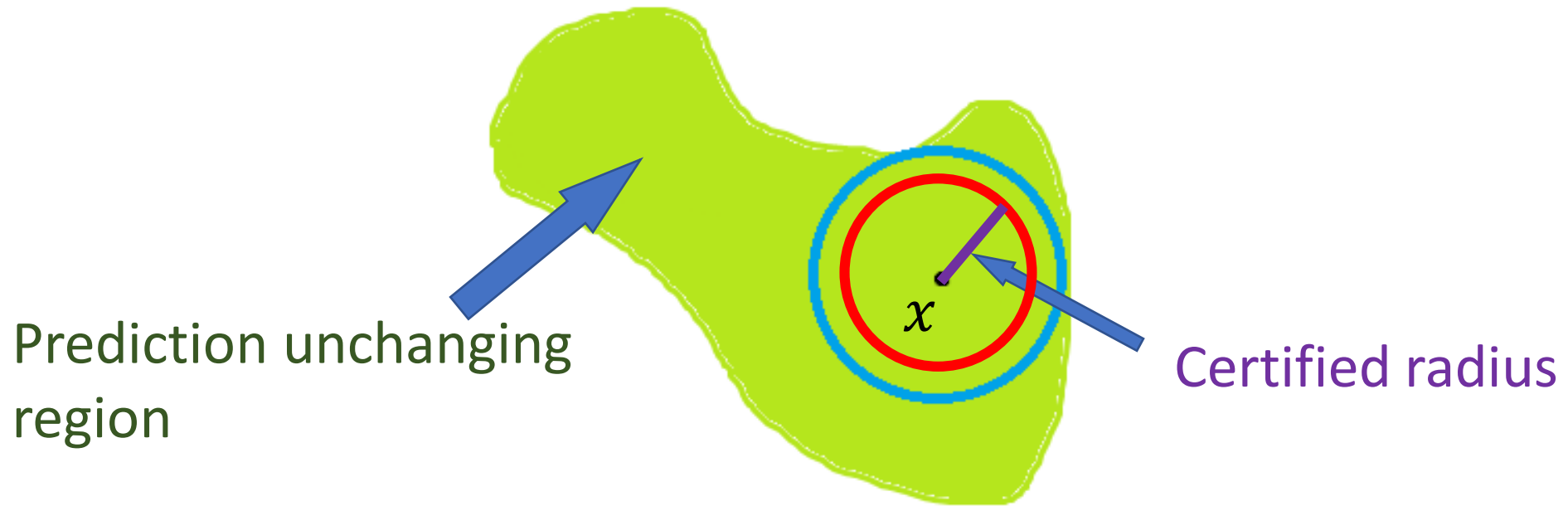
Computing the robust radius is NP-hard



Certified radius

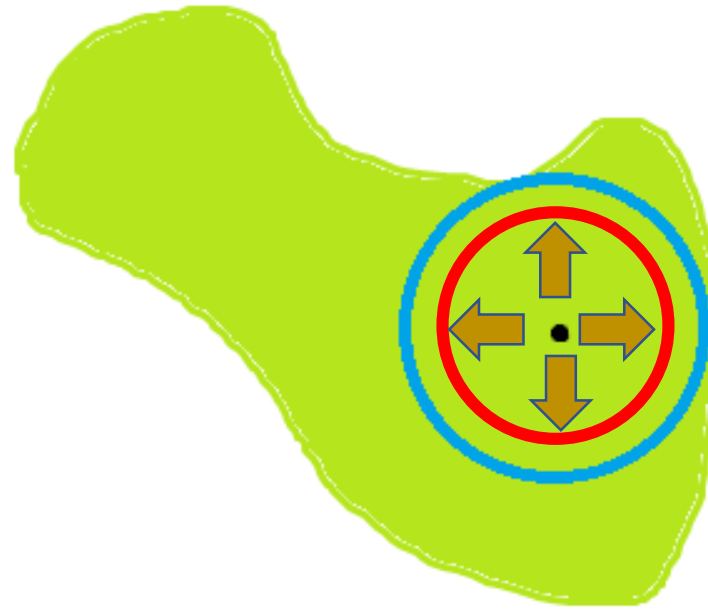
Certified radius: a lower bound of the robust radius

Can be efficiently computed with a certification method



MACER: MAXimizing the CERtified Radius

MACER indirectly maximizes the robust radius

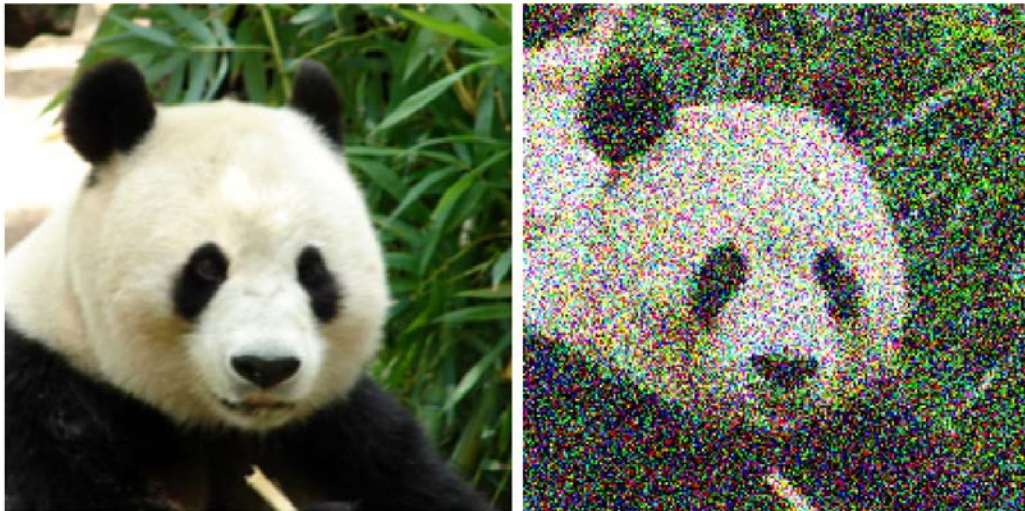


Computing the certified radius via Randomized Smoothing¹

Smoothed classifier $g(x)$

Base classifier $f(x)$

$$g(x) = \operatorname{argmax}_c P_{\eta \sim N(0, \sigma^2 I)}(f(x + \eta) = c)$$



Randomized Smoothing Theorem: The certified radius of $g(x)$ is

$$\frac{\sigma}{2} \left[\Phi^{-1} \left(P_{\eta \sim N(0, \sigma^2 I)}(f(x + \eta) = y) \right) - \Phi^{-1} \left(\max_{c \neq y} P_{\eta \sim N(0, \sigma^2 I)}(f(x + \eta) = c) \right) \right]$$

where Φ is the c.d.f. of the standard Gaussian distribution

¹ Cohen et al., Certified Adversarial Robustness via Randomized Smoothing, ICML 2019.

Step 1: Surrogate loss

0/1 robust classification error:

$$\max_{\|\delta\| \leq \epsilon} \mathbf{1}_{\{f(x+\delta) \neq y\}}$$

Surrogate loss: Classification loss Robustness loss

$$\mathbf{1}_{\{g(x) \neq y\}} + \mathbf{1}_{\{g(x) = y, CR(g; x, y) < \epsilon\}}$$

where $CR(g; x, y)$ is the certified radius

Step 2: Differentiable certified radius

We introduce **soft randomized smoothing** to make the certified radius differentiable

- Original (hard) randomized smoothing:

$$g(x) = \operatorname{argmax}_c P_{\eta \sim N(0, \sigma^2 I)}(f(x + \eta) = c)$$

- Soft randomized smoothing:

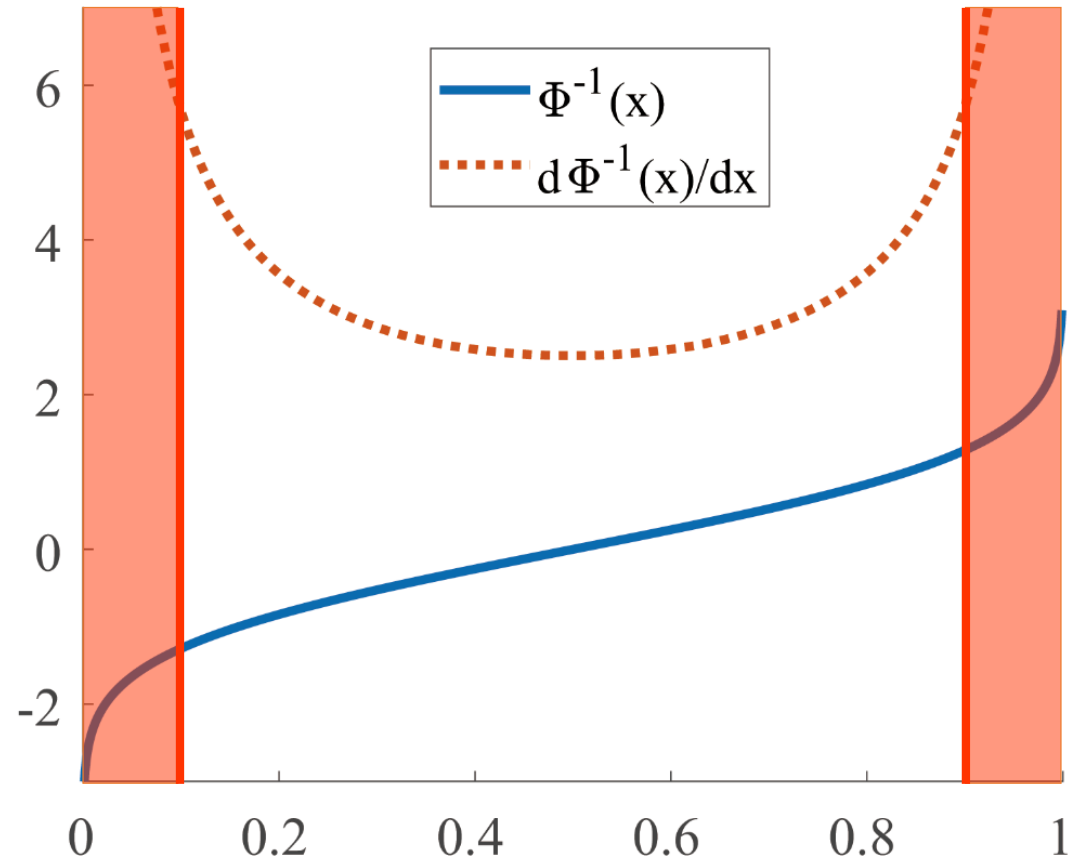
$$\tilde{g}(x) = \operatorname{argmax}_c \mathbb{E}_{\eta \sim N(0, \sigma^2 I)} \boxed{z^c(x + \eta)}$$

Softmax output

Step 3: Numerical stability

Use hinge loss to maintain numerical stability

$\Phi^{-1}(x)$ has exploding gradients near 0 and 1



Experimental results

Better performance and faster speed than previous work

Table 3: Training time and performance of $\sigma = 0.25$ models.

Dataset	Model	sec/epoch	Epochs	Total hrs	ACR
Cifar-10	Cohen-0.25 (Cohen et al., 2019)	31.4	150	1.31	0.416
	Salman-0.25 (Salman et al., 2019)	1990.1	150	82.92	0.538
	MACER-0.25 (ours)	504.0	440	61.60	0.556
ImageNet	Cohen-0.25 (Cohen et al., 2019)	2154.5	90	53.86	0.470
	Salman-0.25 (Salman et al., 2019)	7723.8	90	193.10	0.528
	MACER-0.25 (ours)	3537.1	120	117.90	0.544

Thank you



Paper



Code